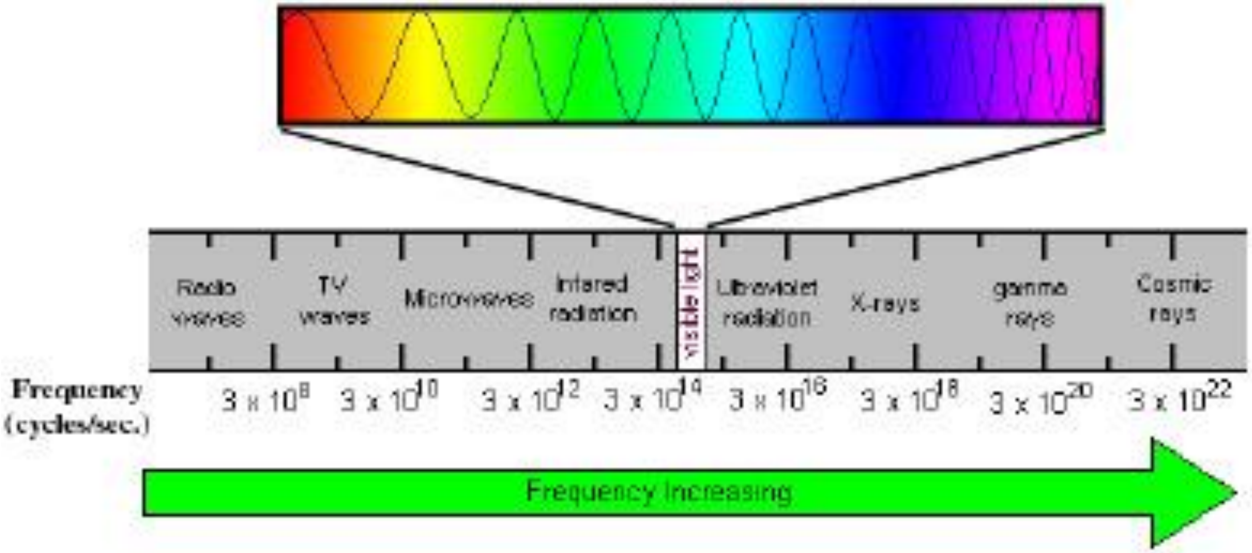
Lecture 5

Digital television

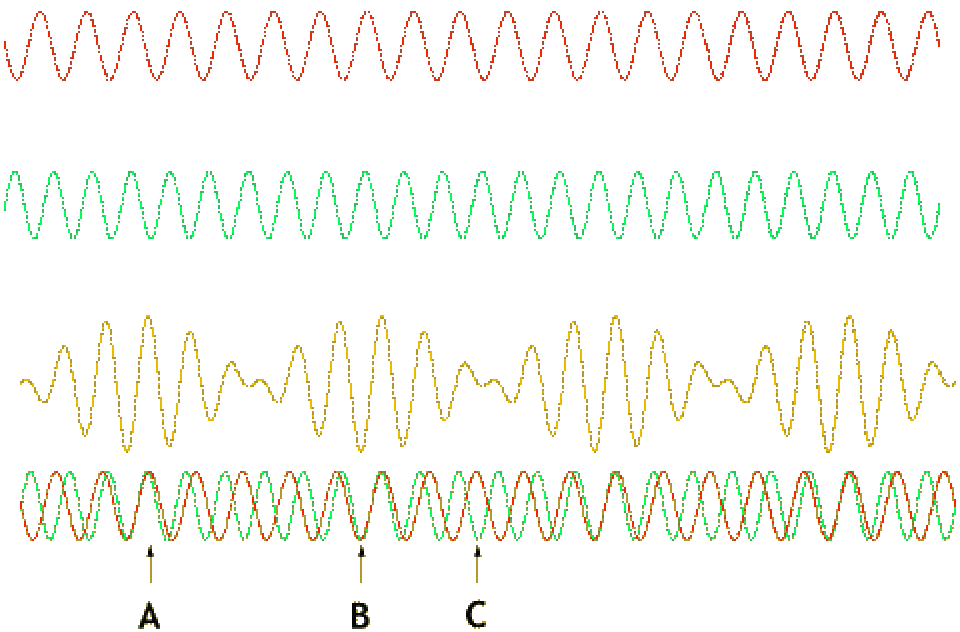
Modulation techniques

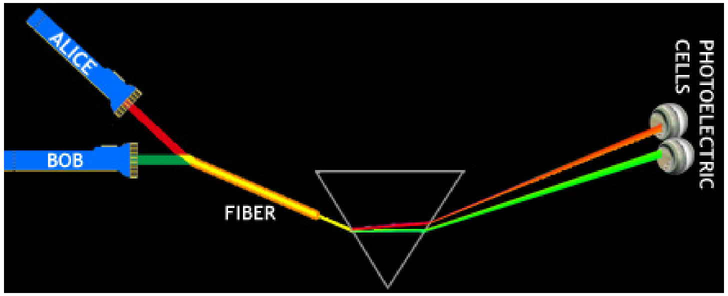
- Electromagnetic waves
- Analog modulation
  - Amplitude modulation
  - Angle modulation
    - Frequency modulation
    - Phase modulation
- Digital modulation
  - On-Off keying
  - Amplitude shift keying
  - Phase shift keying
  - Quadrature amplitude modulation

Electromagnetic waves



Electromagnetic waves





Modulation

"modulate" is "To adjust or adapt to a certain proportion."

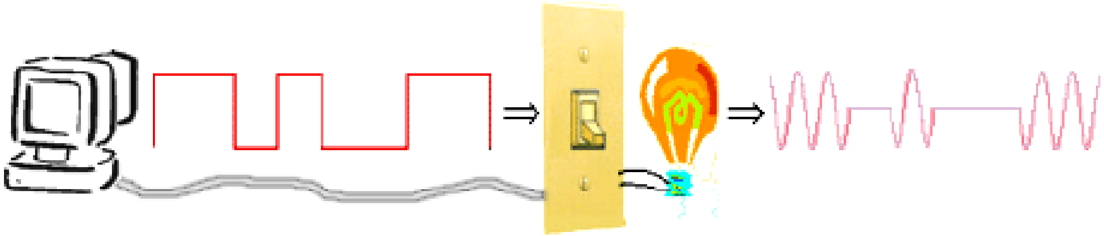
”Linear” modulation

$$x_c(t) = A_c\left(1 + \mu x(t)\right)\cos\omega_c t$$

Exponential modulation

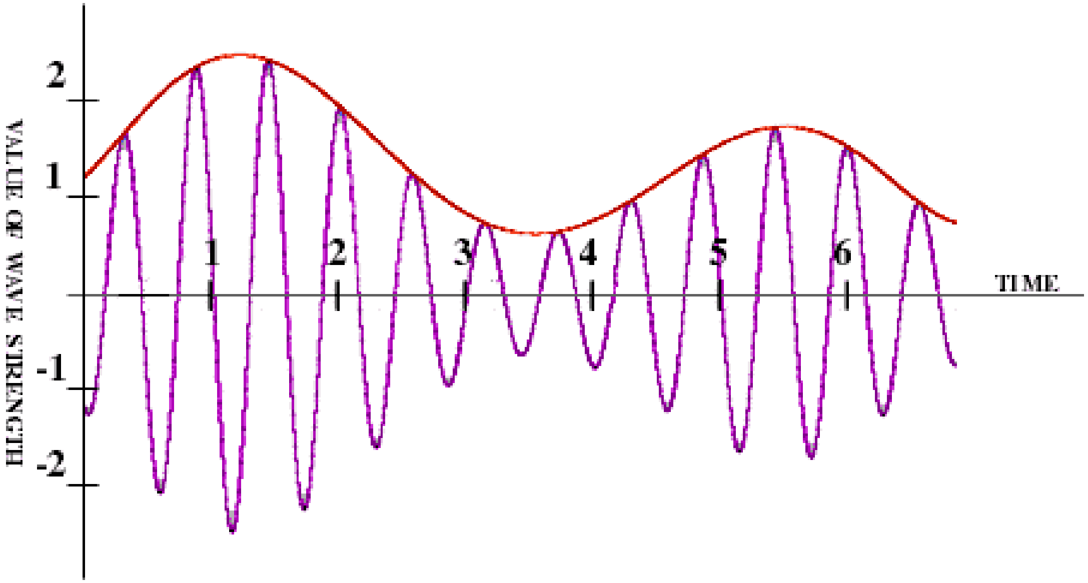
$$\begin{aligned} x_c(t) &= A_c \cos\left(\omega_c t + \phi(t)\right) \\ &= A_c \cos\Theta_c(t) = A_c \operatorname{Re}\left[e^{j\Theta_c(t)}\right] \end{aligned}$$

Amplitude modulation



E.g..
- AM radio stations
- Analog television

Amplitude modulation



$$x_c(t) = A_c m(t) \cos 2\pi f_c t \qquad (3.1)$$

$$X_c(f) = \frac{A_c}{2}\left[M(f+f_c) + M(f-f_c)\right] \qquad (3.2)$$

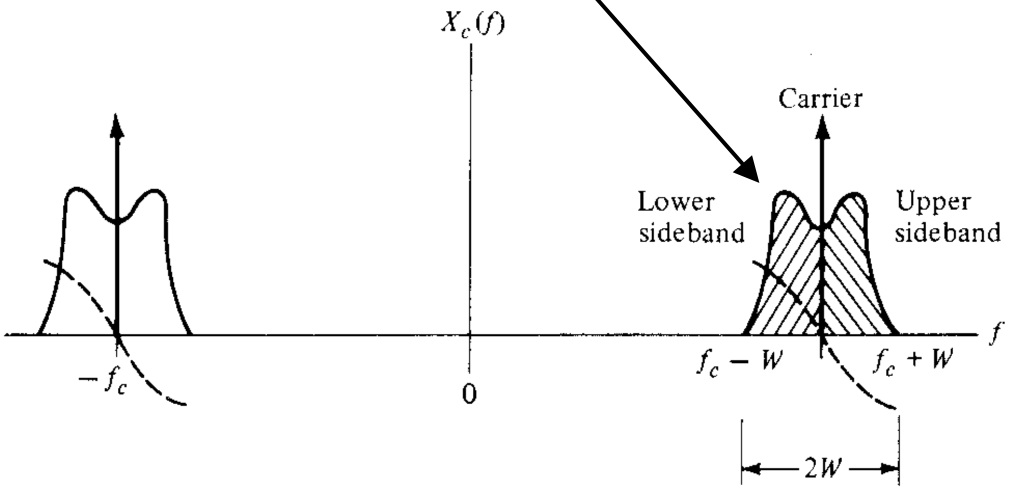
AM: waveforms and bandwidth

- AM in frequency domain:

$$x_C(t) = A_C[1+\mu x_m(t)]\cos(\omega_C t)$$
$$= \underbrace{A_C\cos(\omega_C t)}_{\text{Carrier}} + \underbrace{\mu x_m(t)\cos(\omega_C t)}_{\text{Information carrying part}}$$

$$X_C(f) = \underbrace{A_C\delta(f-f_C)/2}_{\text{Carrier}} + \underbrace{\mu A_C X_m(f-f_C)/2}_{\text{Information carrying part}} \quad f>0\,(\text{for brief notations})$$

- AM bandwidth is twice the message bandwidth *W*:



Phase modulation (PM)

Åbo Akademi University

- Carrier Wave (CW) signal: $x_c(t) = A_c \cos(\underbrace{\omega_c t + \phi(t)}_{\theta_c(t)})$
- In exponential modulation the modulation is "in the exponent" or "in the angle"

$$x_c(t) = A_c \cos(\theta_c(t)) = A_c \operatorname{Re}[\exp(j\theta_c(t))]$$

- Note that in exponential modulation superposition does not apply:

$$x_c(t) = A\cos\{\omega_c t + k_f[a_1(t) + a_2(t)]\}$$

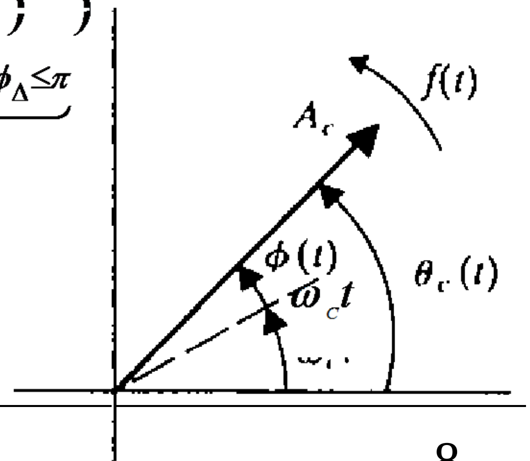
$$\neq A\cos\omega_c t + A\cos k_f[a_1(t) + a_2(t)]$$

- In **phase modulation** (PM) carrier phase is linearly proportional to the modulation amplitude:

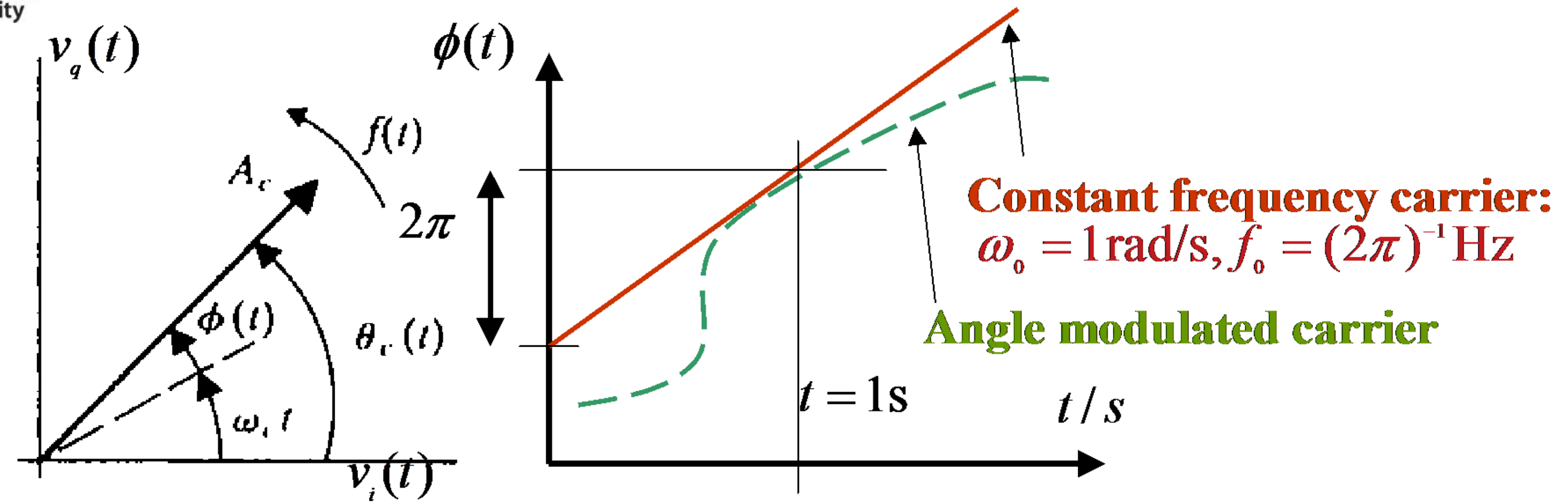
$$x_{PM}(t) = A_c \cos(\underbrace{\omega_c t + \overbrace{\phi(t)}^{\phi_\Delta x(t), \phi_\Delta \le \pi}}_{\theta_C(t)})$$

- Angular phasor has the instantaneous frequency (*phasor rate*)

$$\omega = 2\pi f(t)$$



Instantaneous frequency



- Angular frequency ω (rate) is the derivative of the phase (the same way as the velocity *v(t)* is the derivative of distance *s(t)*)
- For continuously changing frequency instantaneous frequency is defined by differential changes:

$$\boxed{\omega(t) = \frac{d\phi(t)}{dt} \qquad \phi(t) = \int_{-\infty}^{t} \omega(\alpha)\,d\alpha}$$

Compare to linear motion: $v(t) = \dfrac{ds(t)}{dt}\left(\approx \dfrac{s_2(t) - s_1(t)}{t_2 - t_1}\right)$

Frequency modulation (FM)

- In frequency modulation carrier instantaneous frequency is linearly proportional to modulation frequency:

$$\omega = 2\pi f(t) = d\theta_C(t)/dt$$
$$= 2\pi[f_C + f_\Delta x(t)]$$

- Hence the FM waveform can be written as

$$x_C(t) = A_C \cos(\underbrace{\omega_C t + 2\pi f_\Delta \int_{t_0}^{t} x(\lambda)d\lambda}_{\theta_C(t)}), t \geq t_0$$

$$\phi(t) = \int_{-\infty}^{t} \omega(\alpha)d\alpha$$

integrate

- Note that for FM

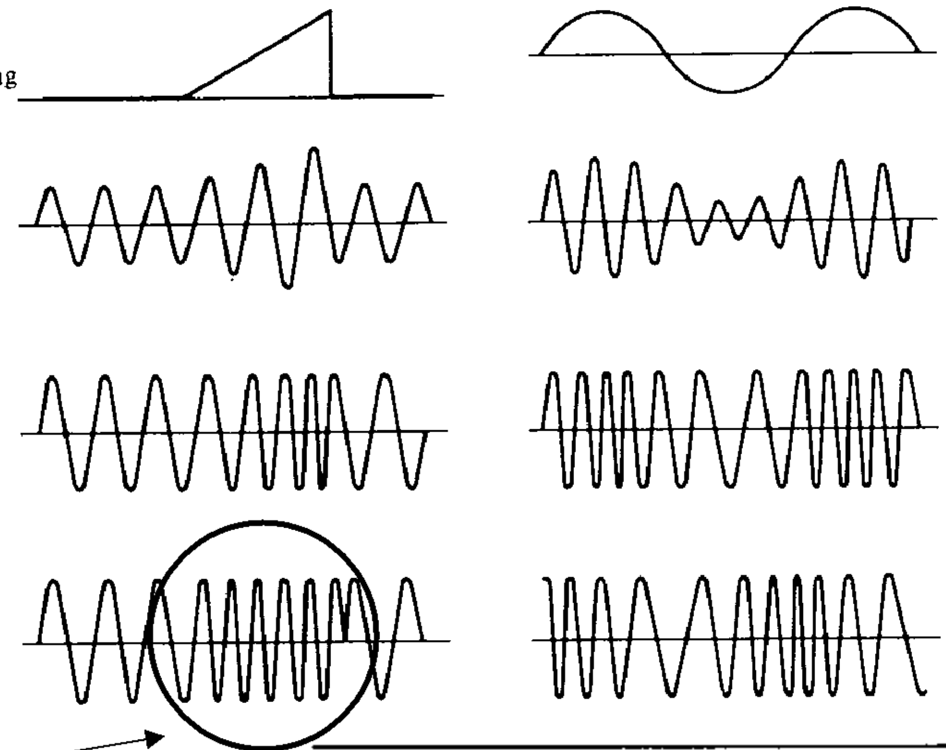
$$f(t) = f_C + f_\Delta x(t)$$

and for PM

$$\phi(t) = \phi_\Delta x(t)$$

	Instantaneous phase $\phi(t)$	Instantaneous frequency $f(t)$
PM	$\phi_\Delta x(t)$	$f_c + \frac{1}{2\pi}\phi_\Delta \dot{x}(t)$
FM	$2\pi f_\Delta \int^t x(\lambda)\,d\lambda$	$f_c + f_\Delta x(t)$

AM, FM and PM waveforms



Constant frequency follows constant modulation waveform derivative

$$x_{PM}(t) = A_c \cos(\omega_c t + \phi_\Delta x(t))$$

$$x_{FM}(t) = A_c \cos(\omega_c t + 2\pi f_\Delta \int^t x(\lambda) d\lambda)$$

	Instantaneous phase $\phi(t)$	Instantaneous frequency $f(t)$
PM	$\phi_\Delta x(t)$	$f_c + \frac{1}{2\pi} \phi_\Delta \dot{x}(t)$
FM	$2\pi f_\Delta \int^t x(\lambda)\, d\lambda$	$f_c + f_\Delta x(t)$

FM Bandwidth

Normally calculated using Carlsons rule

$B = 2\,(D + 1)W$

where W is the maximun modulation frequency and
D is the devation rato $D = f_\Delta / W$

f_Δ is the peak frequency deviation

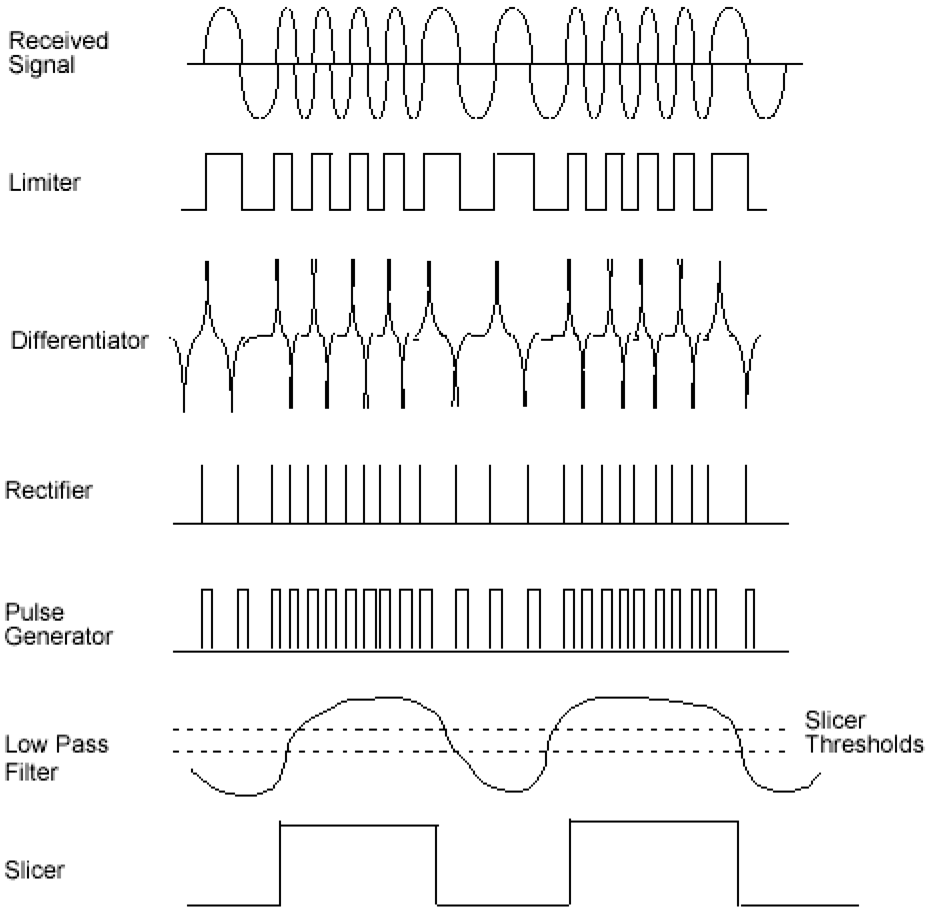
FM Radio: $f_\Delta = 75$ kHz, $W = 15$ kHz

$B = 2 * (75 / 15 + 1) * 15$ kHz$= 180$ kHz

FM demodulation - Example

Zero-crossing based demodulation

Other:
PLL



Comparison of carrier wave modulation systems

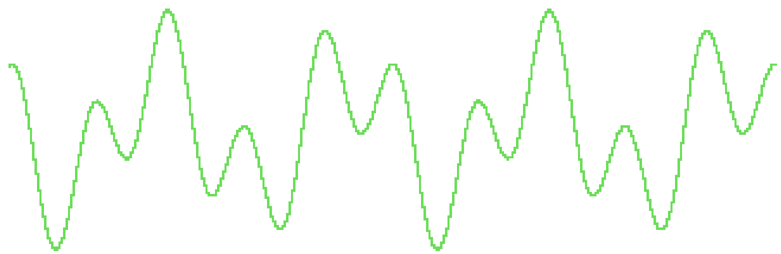
Type	$b = B_T/W$	$(S/N)_D/\gamma$	γ_{th}	DC	Complexity	Comments	Typical applications
Baseband	1	1	...	No†	Minor	No modulation	Short-haul links
AM	2	$\frac{\mu^2 S_x}{1+\mu^2 S_x}$	20	No	Minor	Envelope detection $\mu \leq 1$	Broadcast ratio
DSB	2	1	...	Yes	Major	Synchronous detection	Analog data, multiplexing
SSB	1	1	...	No	Moderate	Synchronous detection	Point-to-point voice, multiplexing
VSB	1+	1	...	Yes	Major	Synchronous detection	Digital data
VSB + C	1+	$\frac{\mu^2 S_x}{1+\mu^2 S_x}$	20	Yes‡	Moderate	Envelope detection $\mu < 1$	Television video
PM§	$2M(\phi_\Delta)$	$\phi_\Delta^2 S_x$	$10b$	Yes	Moderate	Phase detection $\phi_\Delta \leq \pi$	Digital data
FM§¶	$2M(D)$	$3D^2 S_x$	$10b$	Yes	Moderate	Frequency detection	Broadcast radio, microwave relay, satellite systems

† Unless direct-coupled.
‡ With electronic DC restoration.
§ $b \geq 2$.
¶ Deemphasis not included.

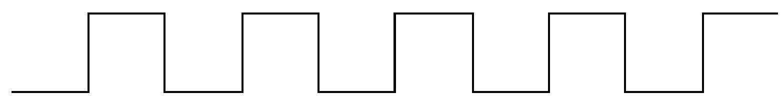
Digital modulation

On-off keying (Binary Amplitude Key Shifting) bandwidth?

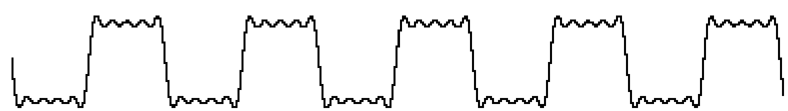
2 analog signals



digital signal (010101...)



digital signal approximated
using 5 sinus waveforms



$$\left[\sin \pi f x + \frac{\sin 3\pi f x}{3} + \frac{\sin 5\pi f x}{5} + \frac{\sin 7\pi f x}{7} + \frac{\sin 9\pi f x}{9}\right]$$ e.g. keeping 5 components -> B = 18 f_m

Shannon's theorem

The capacity *C* of a channel is

$$C = B \log_2 \left(1 + \frac{S}{N}\right).$$

where *B* is the bandwidth and S/N is the signal to noise ratio (given in watts/watts)

The dB scale:

$$SNR_{dB} = 10 \log_{10} (SNR) \text{ (dB)}$$

PAL analog 8MHz studio eq. S/N = 65 dB -> 149 Mbit/s
PAL analog 8MHz broadcast S/N = 21 dB -> 59 Mbit/s

Practical for digital applications 15 dB -> 30 Mbit/s

Normal digital applications: 6 bps / Hz

Short notes on dB

- Generally: magnitude of a physical quantity (usually power or intensity) relative to a certain reference value
- i.e. signal (*S*) to noise (*N*) – *S*/*N* – given in dB form

  $SNR_{dB} = 10 \log_{10} (S/N)$ (dB)

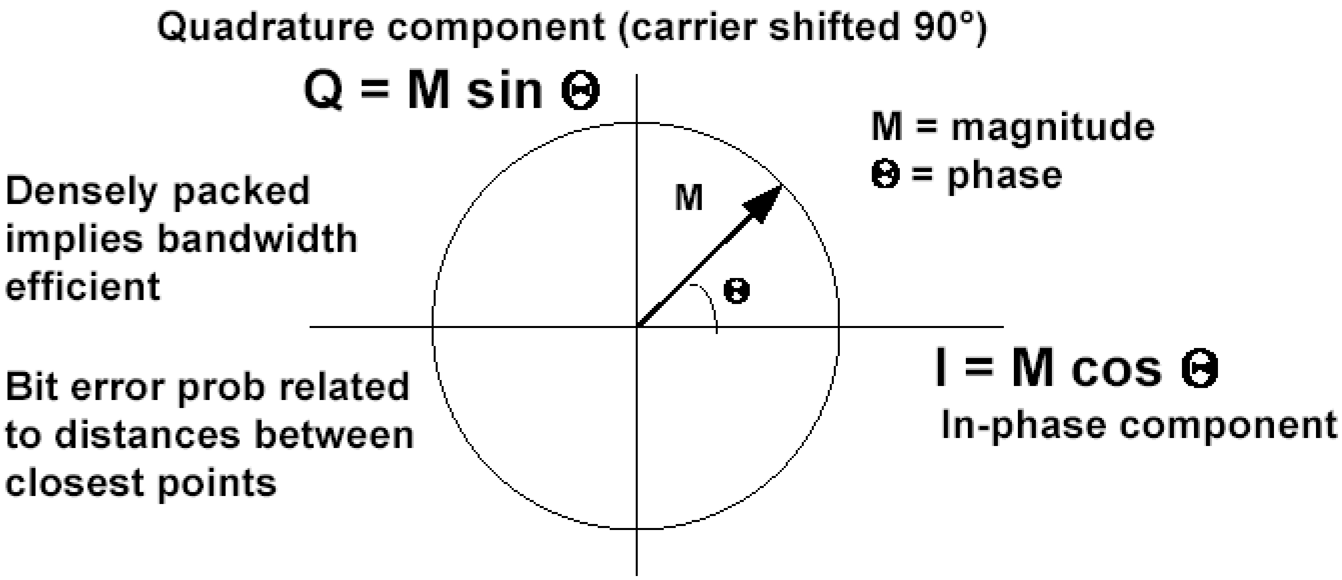
  e.g. $SNR_{dB} = 0$ dB → $S/N = 1$

  $SNR_{dB} = 2$ dB → $S/N = 10\text{^}(2/10) = 1{,}58$

- Voltage
  - dBv – voltage relative to 1 V
  - dBmV – voltage relative to 1 mV
- Radio power
  - dBm – (also dBmW) power ratio in decibels (dB) of

Digital modulation

- Modify carriers amplitude and/or phase (and frequency)
- Constellation: Vector notation / polar coordinates

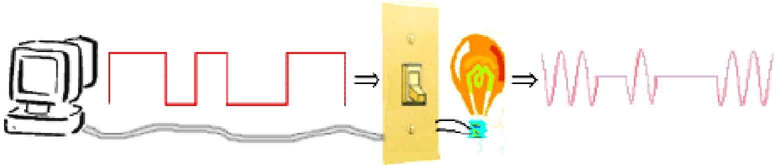


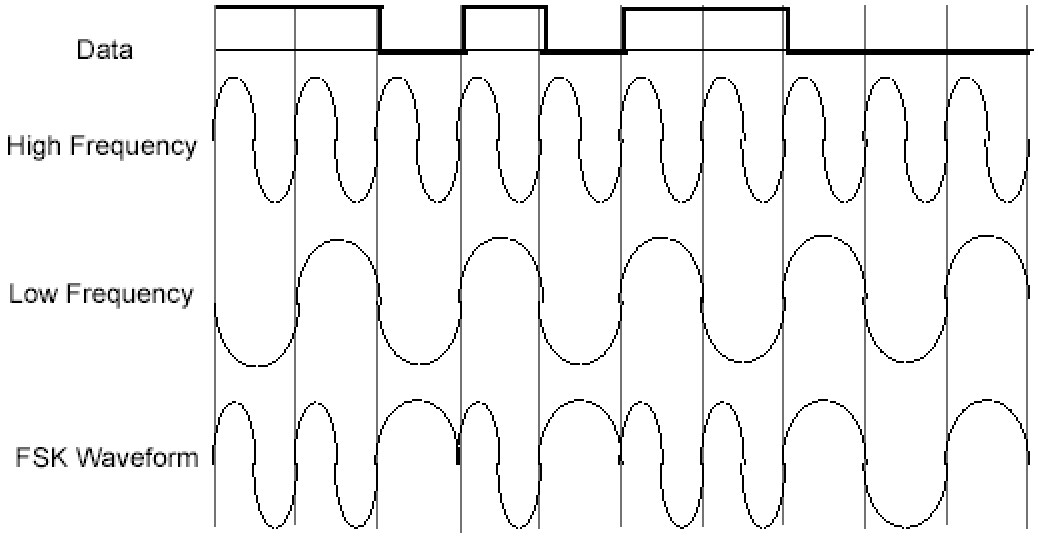
Modulation scheme - considerations

- High spectral efficiency
- High power efficiency
- Robust to multipath effects
- Low cost and ease of implementation
- Low carrier-to-cochannel interference ratio
- Low out of band radiation
- Constant or near constant envelope
  - Constant: Only phase is modulated
  - Non-constant: phase and amplitude is modulated

Binary modulations

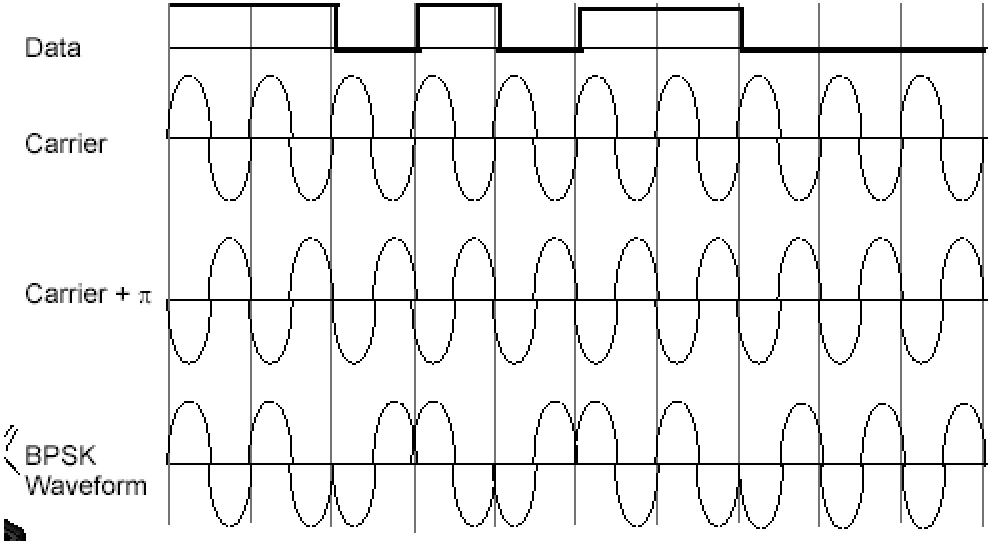
- Amplitude shift keying (ASK)
  Transmission on-off
- Frequency shift keying (FSK)

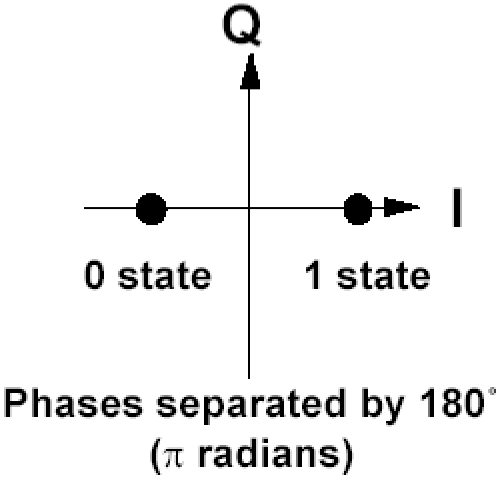




Binary modulations

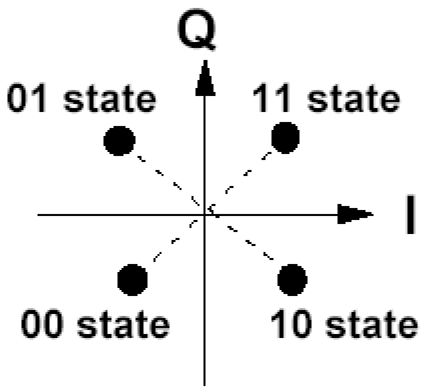
- Binary phase shift keying (BPSK)
  - Simple to implement, inefficient use of bandwidth
  - Very robust, used in satellite communications





Phase key shifting

- Quadrature Phase Shift Keying (QPSK)
  - Multilevel modulation technique: 2 bits per symbol
  - More spectral efficiency, more complex receiver

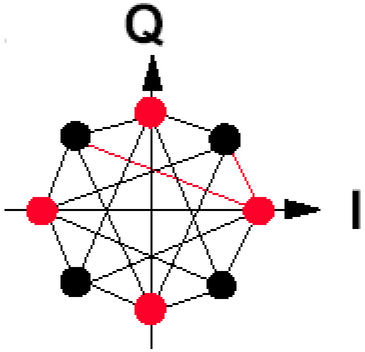


Phase of carrier:
$\pi/4$, $3\pi/4$, $5\pi/4$, $7\pi/4$

Output waveform is sum of modulated ± Cosine and ±Sine wave

π / 4 – Shifted QPSK

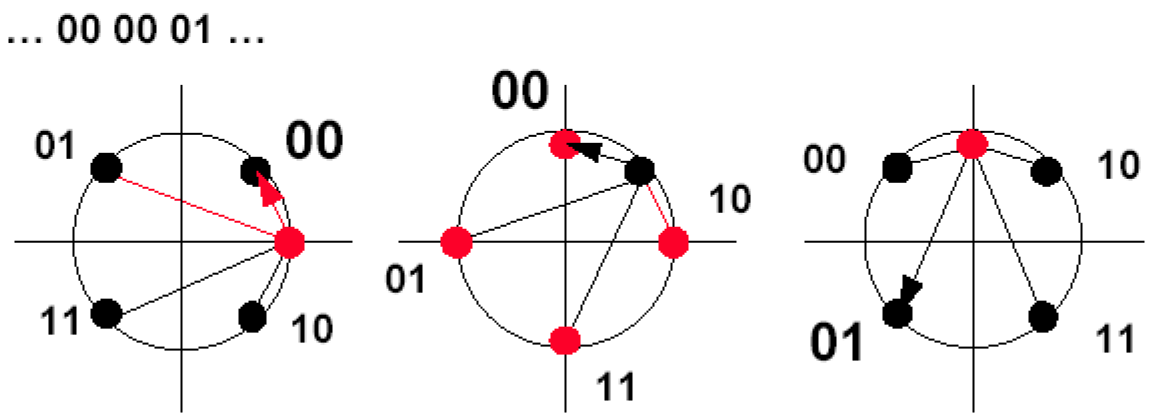
- Variation of QPSK
  - Restricted carrier phase transitions to +/- $\pi/4$ and +/- $3\pi/4$
  - Signalling elements selected in turn from two QPSK constellations each shifted by $\pi/4$
- Popular in Second Generation Systems
  - North American Digital Cellular (1.62 bps / Hz)
  - Japanese Digital Cellular System (1.68 bps / Hz)



π / 4 – Shifted QPSK

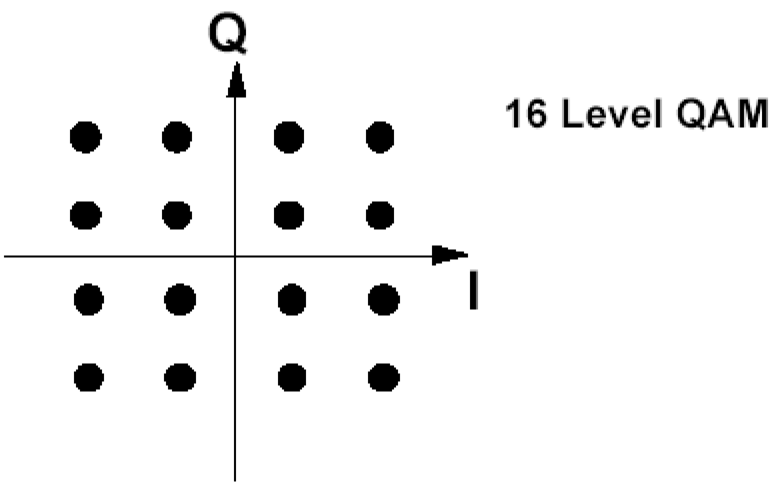
- Advantages
    - Two bits per symbol
    - Phase transitions avoid center of diagram, remove som design constraints on receiver
    - Always a phase change between symbols, leading to self-clocking

Data	Phase Change
00	45°
01	135°
10	-45°
11	-135°



Quadrature Amplitude Modulation

- Quadrature Amplitude Modulation (QAM)
    - Amplitude modulation on both quadrature carriers
    - 2^n discrete levels, if n=2 -> same as QPSK
- Extensively used in microwave links
- DVB-T uses QAM



Quadrature Amplitude Modulation

4 bits / symbol

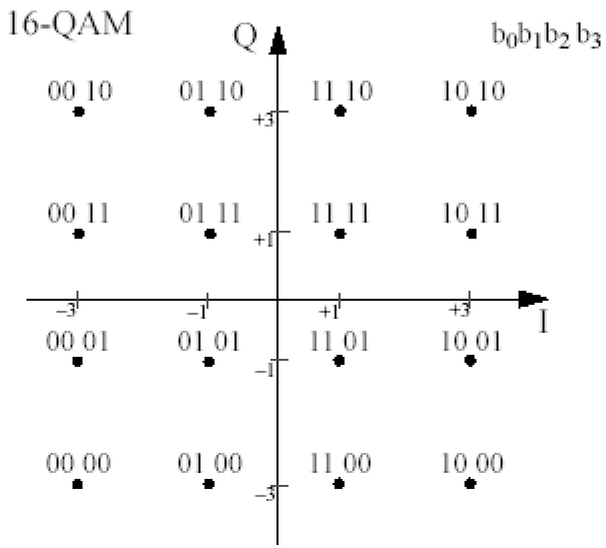


Table 84—16-QAM encoding table

Input bits (b_0 b_1)	I-out
00	–3
01	–1
11	1
10	3

Input bits (b_2 b_3)	Q-out
00	–3
01	–1
11	1
10	3

Quadrature Amplitude Modulation

6 bits / symbol

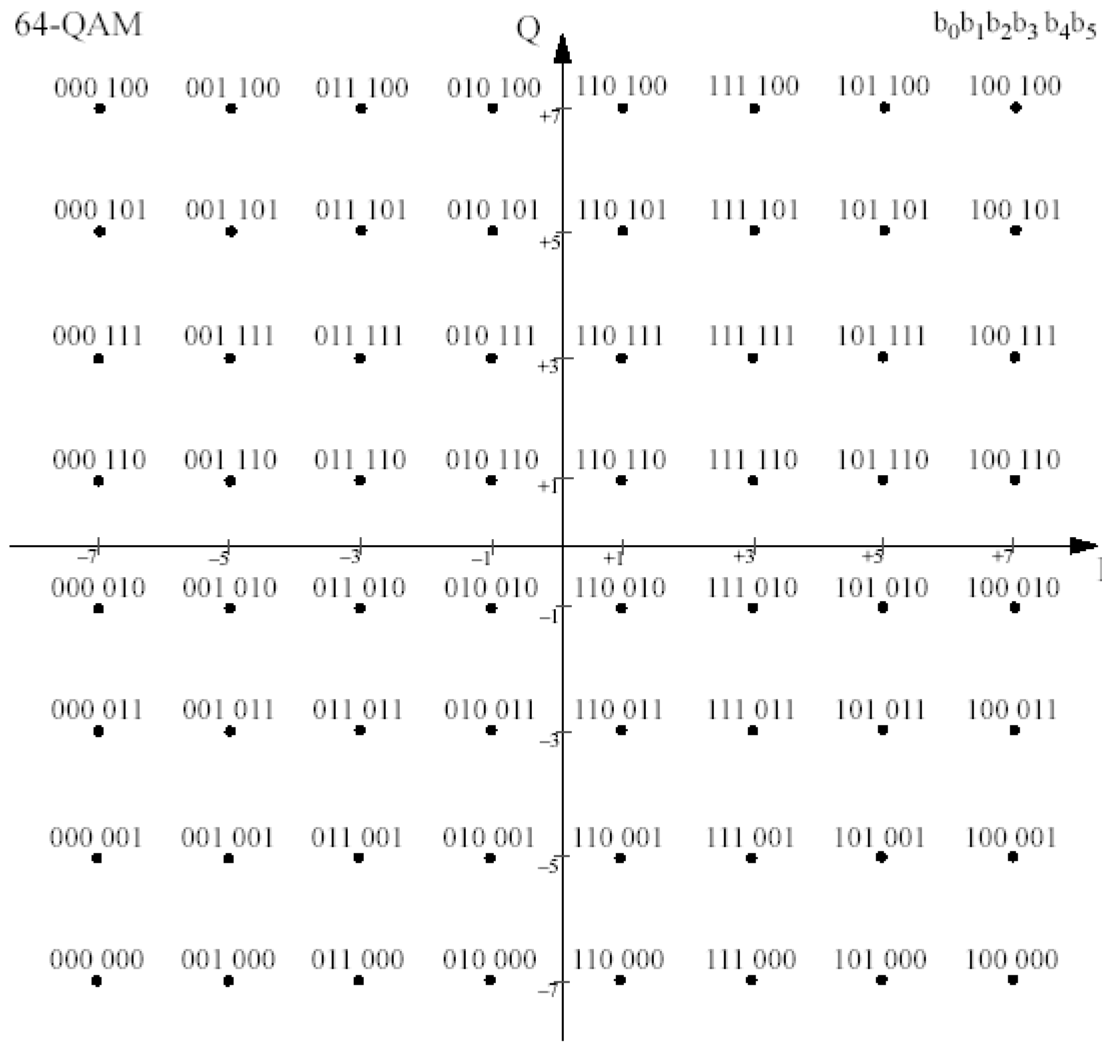


Table 85—64-QAM encoding table

Input bits (b_0 b_1 b_2)	I-out
000	–7
001	–5
011	–3
010	–1
110	1
111	3
101	5
100	7

Input bits (b_3 b_4 b_5)	Q-out
000	–7
001	–5
011	–3
010	–1
110	1
111	3
101	5
100	7

Gray coding

- Present integers, represented in binary format, in such and order, that adjacent integers differ only in one position
- In QAM modulation, c are usually represente
- Now, hamming distanc represent physical dist between constellation